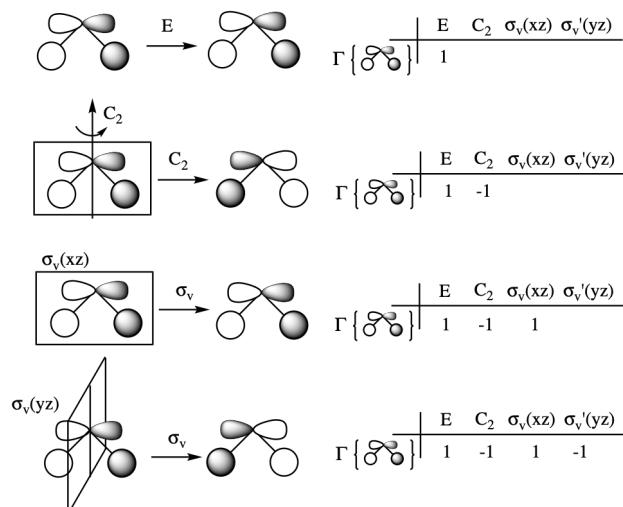


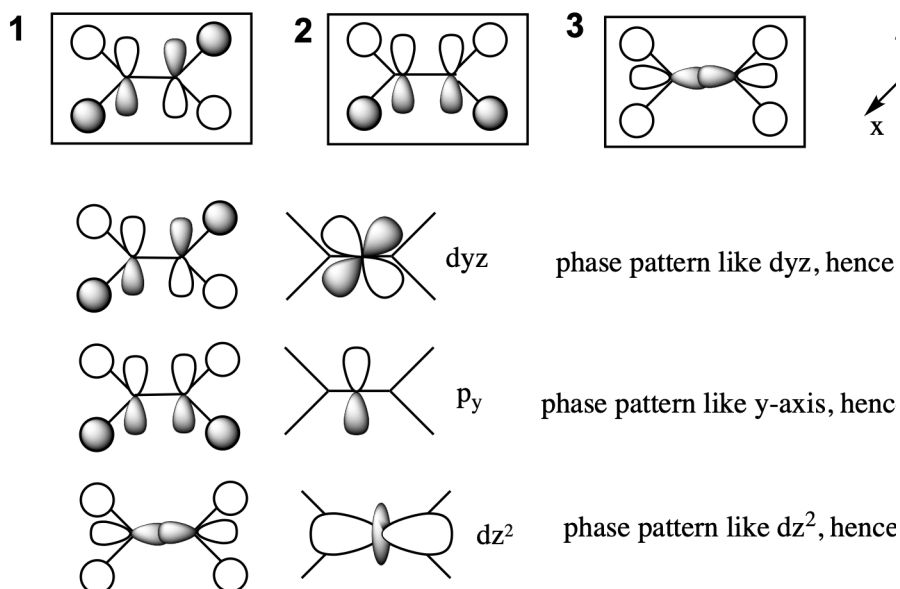
## In-Class Problems / Self-study Problems / Test Preparation: Lecture 2

- **In-Class P1** Use a representation table to determine the symmetry label for MO2.



**Figure 1** Filling out the representation table for MO2

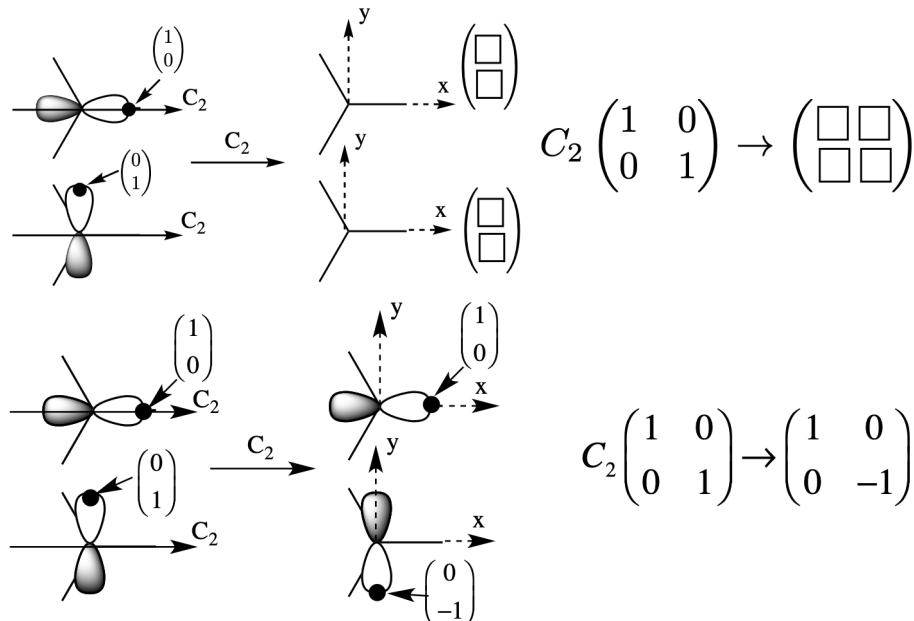
- matching the representation table against the  $C_{2v}$  point group table we see that MO2 has  $b_1$  symmetry (note the small letter!)
- **In-Class P2** for What is the symmetry of the  $p_x$  and  $p_y$  AOs of Pt? and What is the symmetry of the  $d_{xy}$  AO of Pt?
  - symmetry of the  $p_x$  and  $p_y$  AOs of Pt is  $eg$
  - symmetry of the  $d_{xy}$  AO of Pt is  $b_2g$
- **In-Class Activity P3** Determine the symmetry of these MOs identifying appropriate "short-cut" through a relationship to cartesian functions.



**Figure 2** Determining orbital symmetry via short-cuts

- In-Class Activity P4** What is the character of the degenerate B  $p_x$  and  $p_y$  AOs under the  $C_2$  axis? Complete the diagram below and determine the transformation matrix and the hence the character.

○ see below the character is the trace =  $1+(-1)=0$

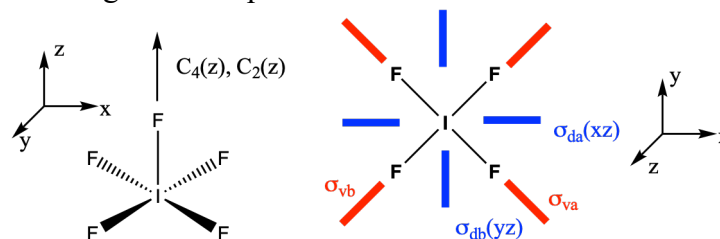


$D_{3h}$	E	$2C_3$	$3C_2$	$\sigma_h$	$2S_3$	$3\sigma_v$	
$A_1'$	1	1	1	1	1	1	
$A_2'$	1	1	-1	1	1	-1	
<b><math>E'</math></b>	2	-1	<b>0</b>	2	-1	0	$(T_x, T_y)$
$A_1''$	1	1	1	-1	-1	-1	
$A_2''$	1	1	-1	-1	-1	1	$T_z$
$E''$	2	-1	0	-2	1	0	

**Figure 3** transformation of the  $p_x$  and  $p_y$  AOs under  $C_2$

- In-Class P5** Draw a Lewis bonding diagram for  $IF_5$  and identify the molecular shape of  $IF_5$  using VSEPR theory. Determine the point group and draw all of the symmetry elements on a diagram of the molecule. Identify if multiple operations in the character table are due to multiple operations on the same element or multiple elements. For the highest rotation axis identify, for any operations that are not-unique, the equivalent operation.

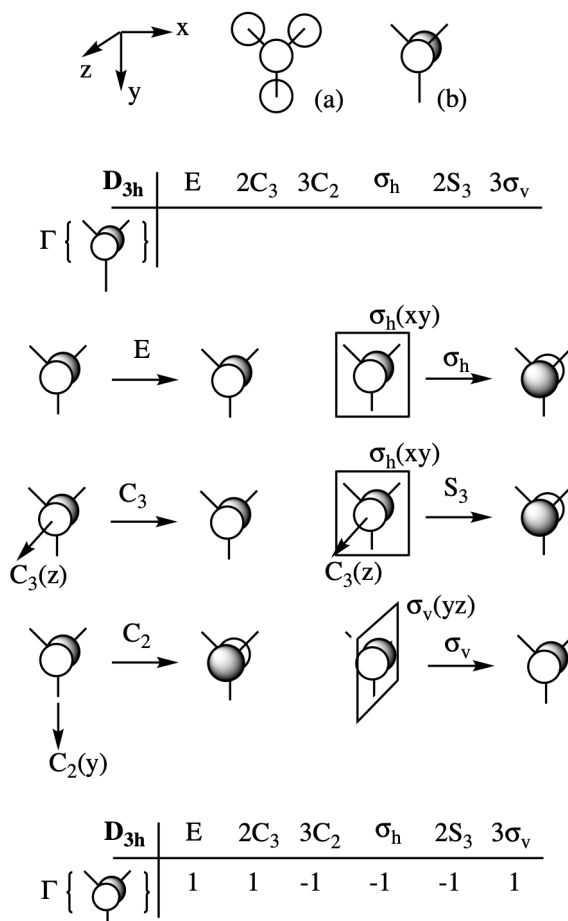
○ each F contributes 7ve 6 of these will be in lone pairs, and 1e will contribute to a covalent bond with I. The I has 7ve, 5 of these will contribute to covalent bonds with the F atoms, 2 will remain non-bonding as a lone pair.



also one F coming out of the page  
(removed for clarity)

**Figure 4** identifying the symmetry operations of  $IF_5$

- point group
    - linear? NO
    - $T_d$  or  $O_h$ ? NO
    - principle axis? YES  $C_4$
    - $4C_2$  perpendicular to  $C_4$ ? NO
    - $\sigma_h$ ? NO
    - $4\sigma_v$ ? YES
    - therefor  $C_{4v}$
  - there are 4 possible  $C_4$  operations  $C_4^1, C_4^2, C_4^3, C_4^4$
  - $C_4^2$  is the same as  $C_2^1$  and  $C_4^4$  is the same as E, therefore  $C_4^1$  and  $C_4^3$  are unique,
  - The  $2C_4$  operations occur around the same element, the  $C_4$  axis
  - the  $2\sigma_d$  and  $2\sigma_v$  operations are due to the presence of different symmetry elements (mirror planes)
- **Q1** determine the symmetry label for the molecular orbitals shown for  $BH_3$  using the "long method" of forming a representation table, for (b) check your answer using a "short-cut" method
- for each example
    1. draw a "representation table" for the MO
    2. determine how the MO transforms under each symmetry operation
    3. compare the representation to the irreducible representations on the character table
  - (a) has  $a_1'$  symmetry
  - (b) has  $a_2''$  symmetry (working shown below) **Figure 5**
  - compare the answer for (b) to the  $T_z$  on  $D_{3h}$  character table which is  $a_2''$  symmetry, **Figure 6**

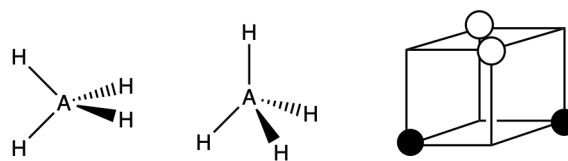


**Figure 5** determining the symmetry label for MO (b)

$D_{3h}$	$E$	$2C_3$	$3C_2$	$\sigma_h$	$2S_3$	$\sigma_v$		
$A_1'$	1	1	1	1	1	1		$x^2 + y^2, z^2$
$A_2'$	1	1	-1	1	1	-1	$R_z$	
$E'$	2	-1	0	2	-1	0	$(T_x, T_y)$	$x^2 - y^2, xy$
$A_1''$	1	1	1	-1	-1	-1		
$A_2''$	1	1	-1	-1	-1	1	$T_z$	
$E''$	2	-1	0	-2	1	0	$(R_x, R_y)$	$xz, yz$

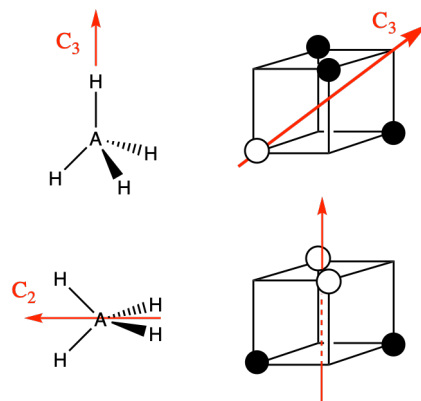
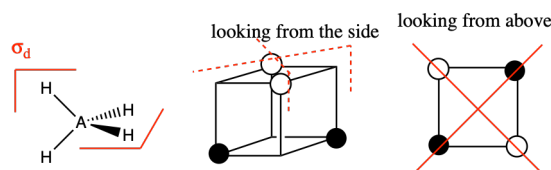
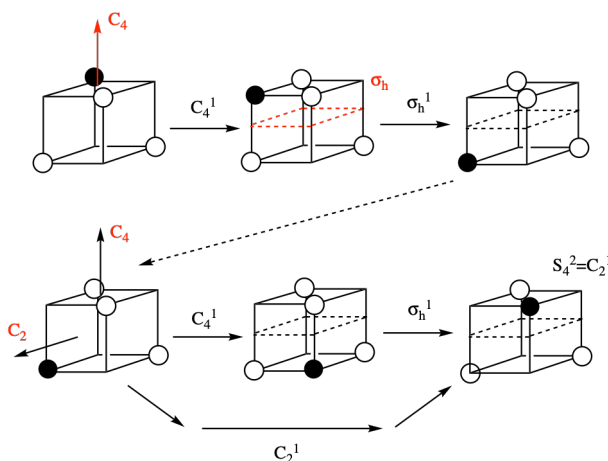
Figure 6  $D_{3h}$  Character Table

- Q2** construct a representation table for the "z-axis" and determine which irreducible representation it transforms as.
  - The z-axis has the same **phase** properties as the  $p_z$  AO of boron and MO(b) above (which is just the  $p_z$  AO of boron, AOs can also be MOs!). Thus we need never actually work out the symmetry labels of the  $p_x$ ,  $p_y$  or  $p_z$  atomic orbitals because they will always have the same symmetry labels as the x, y and z axes. The representation table is therefore the same as that for the  $p_z$  orbital and the symmetry label is  $a_2''$ .
- Q3** *In your own words*, using bullet points, write out the general procedure to determine the symmetry label of a molecular orbital. This is my process however you should go through the notes and an example and write out the process **for yourself in your own words!**
  - determine the point group of the molecule
  - define the axis system
  - draw a representation table for the MO
  - determine how the MO transforms under each symmetry operation
  - enter +1 for no phase change, -1 for a phase change
  - compare this representation to the irreducible representations from the character table
  - use a small letter for the symmetry label of a MO
- Q4** *In your own words*, using bullet points, write out the general procedure to determine the character of a degenerate set of orbitals? This is my process however you should go through the notes and an example and write out the process for yourself in your own words!
  - take point on tip of each orbital
  - form the starting matrix
  - perform the symmetry operation on the orbitals
  - write coordinates of each point
  - form the final matrix by combining the coordinates
  - the character is the TRACE of the final matrix
- Q5** The Tetrahedral Point Group (*advanced!*)
  - discuss and illustrate the symmetry operations of the  $T_d$  point group.
  - hint:** there are three useful ways of thinking about a tetrahedral molecule, **Figure 7**, each one emphasises a different aspect of symmetry:
    - the  $C_2$  axes
    - the  $C_3$  axes
    - the cubic structure

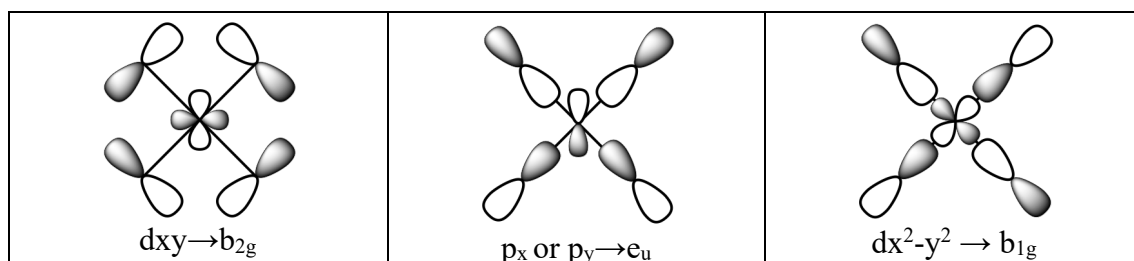
Figure 7 different ways to represent a  $T_d$  molecule

- the "cube" may be less familiar to you, think of the H atoms occupying opposite corners of a cube and the central atom A is at the center of the cube
- The character table for the  $T_d$  point group is shown to the left, **Figure 8** and it tells us the key symmetry operations in this group are E,  $8C_3$ ,  $3C_2$ ,  $6S_4$  and  $6\sigma_d$
- there are  $8C_3$  operations
  - a  $C_3$  axis lies along each bond, one  $C_3$  axis is shown in **Figure 9**, the others are easily predicted because the four H atoms are symmetry equivalent, if one H atom has a  $C_3$  axis passing through it then they all will, hence there are four  $C_3$  axis symmetry elements
  - around each axis there are 3 possible  $C_3$  operations:  $C_3^1$ ,  $C_3^2$ ,  $C_3^3$ , the last operation  $C_3^3 = E$  is equivalent to the identity and so is already counted, there are then two symmetry operations associated with each  $C_3$  axis
  - thus there are eight distinct  $C_3$  operations in  $T_d$ :  $8C_3$
- there are  $3C_2$  operations
  - a  $C_2$  axis lies between each pair of A-H bonds, **Figure 9**, bisecting each pair of atoms and through the center of each pair of faces in the cube, as there are 3 pairs of faces to each cube, there will be  $3C_2$  axes
  - as we associate only one operation with each  $C_2$  axis there are 3  $C_2$  operations in  $T_d$
- there are  $6\sigma_d$  operations
  - a  $\sigma$  mirror plane passes through each pair of atoms and contains a  $C_2$  axis, ie two mirror planes cross each pair of faces, **Figure 10**, these are dihedral mirror planes  $\sigma_d$ .
  - as there are 3 pairs of faces each with two mirror planes there are  $6\sigma_d$  operations in  $T_d$
- there are  $6S_4$  operations
  - each  $C_2$  axis has a coincident  $S_4$  axis, consider a rotation of  $90^\circ$  around this axis and then reflection in a plane perpendicular to the axis through the center of the molecule.
  - An example of these elements for the  $S_4^1$  operation is given in **Figure 11**

$T_d$	E	$8C_3$	$3C_2$	$6S_4$	$6\sigma_d$	h=24
$A_1$	1	1	1	1	1	
$A_2$	1	1	1	-1	-1	
E	2	-1	2	0	0	
$T_1$	3	0	-1	1	-1	
$T_2$	3	0	-1	-1	1	( $T_x T_y T_z$ )

**Figure 8**  $T_d$  character table**Figure 9**  $T_d$  rotation operations**Figure 10**  $T_d$   $\sigma_d$  mirror plane**Figure 11** top is the  $S_4^1$  operation, followed by the  $S_4^2$  operation on the bottom

- I am rotating counter clockwise, I can rotate in any direction I like as long as I am consistent for all operations. If I call counter-clockwise the positive direction, then rotating in the opposite direction becomes the "reverse" operation of  $C_4^{-1}$ .
- after the  $C_4^1$  operation the "atom" is now "off" the molecule! However, once the whole  $S_4^1$  operation is completed it is back "on" the molecule. This is a consequence of **neither the  $C_4$  nor the  $\sigma_h$  existing within the  $T_d$  point group as separate elements!!**
- $S_4^2$  ( in **Figure 11**) is the same as  $C_2$  operation and  $C_2$  lies to the left of  $S_4$  in the character table and so this operation is not counted with the  $S_4$  operations. In addition the  $S_4^4$  operation is the same as E and so is not counted either
- thus there are  $2S_4$  operations per  $C_2$  axis, and as there are  $3C_2$  axes there must be  $6S_4$  operations in  $T_d$
- Thus we have shown that there are E,  $8C_3$ ,  $3C_2$ ,  $6S_4$  and  $6\sigma_d$  operations for the  $T_d$  point group.
- **Q6** Identify the symmetry of the following MOs of a  $D_{4h}$  molecule, use the short-cuts where possible



$D_{4h}$	E	$2C_4$	$C_2$	$C_2'$	$C_2''$	$i$	$2S_4$	$\sigma_h$	$2\sigma_v$	$2\sigma_d$	
$A_{1g}$	1	1	1	1	1	1	1	1	1	1	$x^2+y^2, z^2$
$A_{2g}$	1	1	1	-1	-1	1	1	1	-1	-1	
$B_{1g}$	1	-1	1	1	-1	1	-1	1	1	-1	$x^2-y^2$
$B_{2g}$	1	-1	1	-1	1	1	-1	1	-1	1	$xy$
$E_g$	2	0	-2	0	0	2	0	-2	0	0	$(xz, yz)$
$A_{1u}$	1	1	1	1	1	-1	-1	-1	-1	-1	
$A_{2u}$	1	1	1	-1	-1	-1	-1	-1	1	1	$T_z$
$B_{1u}$	1	-1	1	1	-1	-1	1	-1	-1	1	
$B_{2u}$	1	-1	1	-1	1	-1	1	-1	1	-1	
$E_u$	2	0	-2	0	0	-2	0	2	0	0	$(T_x, T_y)$

Figure 12  $D_{4h}$  character table